

- Q1. Two windings one mounted on the stator and the other mounted on the rotor have self and mutual inductance of $L_{11} = 4.5$ H, $L_{22} = 2.5$ H and $L_{12} = L_{21} = 2.8 \cos \theta$ H, where $\theta = \omega_m t + \delta$ is the angle between the axis of the winding. Let the current in the first winding be denoted by i_1 and the current in the second winding by i_2 . Derive an expression for the instantaneous torque as a function of the angular position θ in simplified form and find the time-average torque for the following conditions:
- $\omega_m = 0$, $\delta = 30^\circ$, $i_1 = 2$ A and $i_2 = 0$ A [2 marks]
 - $\omega_m = 0$, $\delta = 30^\circ$, $i_1 = i_2 = 2$ A [2 marks]
 - $\omega_m = 0$, $\delta = 30^\circ$, $i_1 = 2$ A and $i_2 = 2\sin 20t$ A. [2 marks]
 - $\omega_m = 0$, $\delta = 30^\circ$, $i_1 = i_2 = 2\sin 20t$ A. [2 marks]
 - $\omega_m = 20$ rad/s, $\delta = 30^\circ$, $i_1 = 2$ A, $i_2 = 2\sin 20t$ A. [2 marks]
- Q2. A magnetic circuit, including a movable plunger, is shown in Figure Q2. Assume that the permeability of the core is infinite and neglect leakage and fringing. The dimensions of magnetic circuit is $a = 2.5$ cm, $b = 2$ cm, $d = 0.02$ cm, $w = 3$ cm (width/thickness of the magnetic core) and numbers of turn of winding, N , is 500 turns.
- Derive an expression for reluctance of magnetic circuit in term of variable x . [2 marks]
 - Write an expression for inductance of magnetic circuit. [2 marks]
 - Derive an expression for field energy stored in the magnetic systems. [2 marks]
 - If exciting current, i , is 5 A, calculate field energy stored at $x = 2$ mm. [2 marks]
 - Derive an expression for the force acting on movable plunger. Calculate the force at $x = 2$ mm. [2 marks]
 - If the armature of the movable plunger moves from open to closed position at constant current, I , as shown in the Figure Q2(g). Show that the electrical energy input is shared equally between field energy stored and mechanical work done. [2 marks]

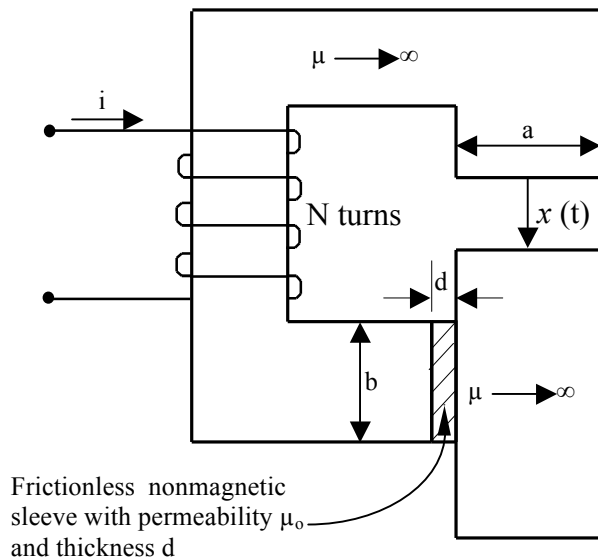


Figure Q2

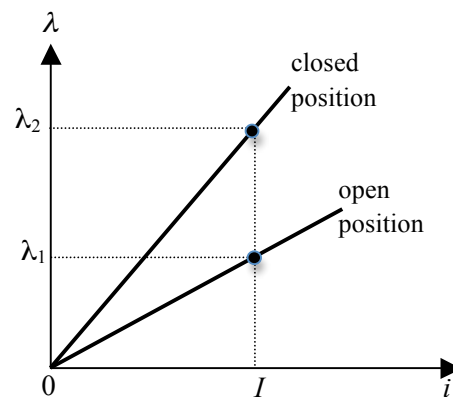


Figure Q2(g)

- Q3. An eight pole DC machine has a lap winding of 400 turns. The flux per pole is 0.05 Wb.
- (i) Determine the generated voltage, E_a , at the speed of 800 rpm. Also, determine the induced voltage for each turn. [3 marks]
 - (ii) Determine the developed torque by the machine if the current through the turn is 5 A at the speed of 800 rpm. [2 marks]
 - (iii) If conductors are available which are rated at 4 V and 10 A, determine the power rating of the machine. [2 marks]
- Q4. A self-excited dc shunt generator 11 kW, 110 V, 1100 rpm has armature resistance $R_a = 0.1 \Omega$, shunt field winding resistance, $R_{fw} = 82 \Omega$ and R_{fc} can be adjusted from 0Ω to 66Ω . The magnetization characteristic curve at 1100 rpm is shown in Figure Q4.
- (i) Draw a self-excited DC shunt generator. Label all resistances, voltages and currents. [2 marks]
 - (ii) Determine the maximum and minimum values of the generated terminal voltage at no load. Draw on the Figure Q4. [3 marks]
 - (iii) Determine the value of the field control resistance, R_{fc} , required to generate rated terminal voltage of 110 V at no load. Draw on the Figure Q4. [2 marks]
 - (iii) Determine the full-load terminal voltage for the value of field control resistance as determined in (ii). Neglect armature reaction effect. Draw on the Figure Q4. [2 marks]
 - (iv) Determine the full-load terminal voltage for R_{fc} as in (ii). Assume that the armature reaction effect at the full-load is $I_{f(AR)} = 0.05$ A. Draw on the Figure Q4. [2 marks]

Your drawing on the Figure Q4 is a part of the solution. You have to submit Figure Q4.

A