

Q1. In an electromagnetic relay system, the flux linkage  $\lambda$  and current  $i$  relationship is given by:

$$i = 2\lambda^2 + 3\lambda(x - 4)^2 + \sin x$$

Evaluate the electromechanical force,  $f_m$  when  $\lambda = 2$  Vs and  $x = 1$  m. [5 marks]

Q2. The magnetic circuit shown in **Figure Q2** is made of high permeability steel so that its reluctance can be negligible. The rotor is free to turn about a vertical axis. The dimensions are shown in the Figure.

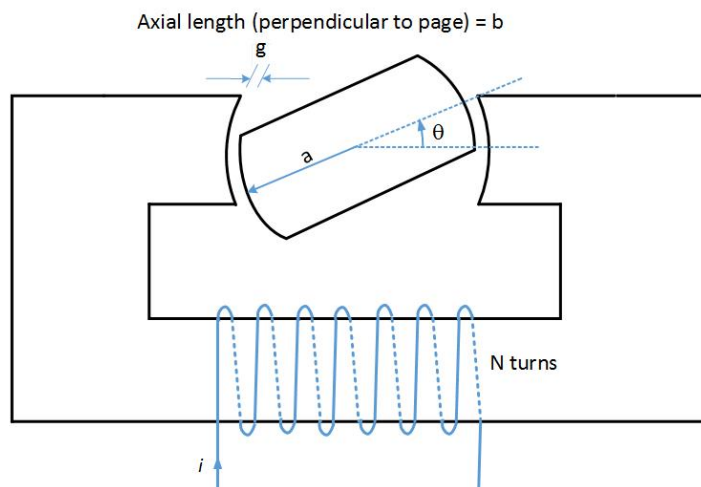


Figure Q2

- (a) Obtain an expression for the effective cross sectional area normal to the flux,  $A_g$ , and the total volume of the air gap,  $V_g$ , as a function of the rotor angle,  $\theta$ , and magnetic circuit dimensions ( $a$ ,  $b$ , and  $g$ , see Figure Q2). [3 marks]
- (b) Obtain an expression for the torque acting on the rotor as a function of the winding current  $i$ , the rotor angle,  $\theta$ , and magnetic circuit dimensions ( $a$ ,  $b$ , and  $g$ , see **Figure Q2**). [3 marks]
- (c) Calculate the torque. Given  $a = 15$  cm,  $g = 2$  mm,  $b = 20$  cm,  $N = 1000$  turns,  $\theta = 30^\circ$ , and  $B = 1$  T. [3 marks]

Q3. An eight-pole, 25-kW, 120-V DC generator has a lap-wound armature, which has 64 coils with 16 turns per coil. Its rated speed is 2400 revolution per minute (rpm).

- (a) How much flux per pole is required to produce the rated voltage in this generator at no-load conditions? [3 marks]
- (b) What is the current for each parallel path in the armature of this generator at the rated load? [2 marks]
- (c) What is the induced torque in this machine at the rated load? [2 marks]
- (e) If the resistance of this winding is  $0.011 \Omega$  is per turn, what is the armature resistance  $R_A$  of this machine? [2 marks]

Q4. An 8 kW, 80 V, 800 rpm dc shunt generator has armature resistance  $R_a = 0.1 \Omega$ , shunt field winding resistance,  $R_{fw} = 70 \Omega$ . The rated field current is 0.8 A. The magnetization characteristic at 800 rpm is shown in **Figure Q4**.

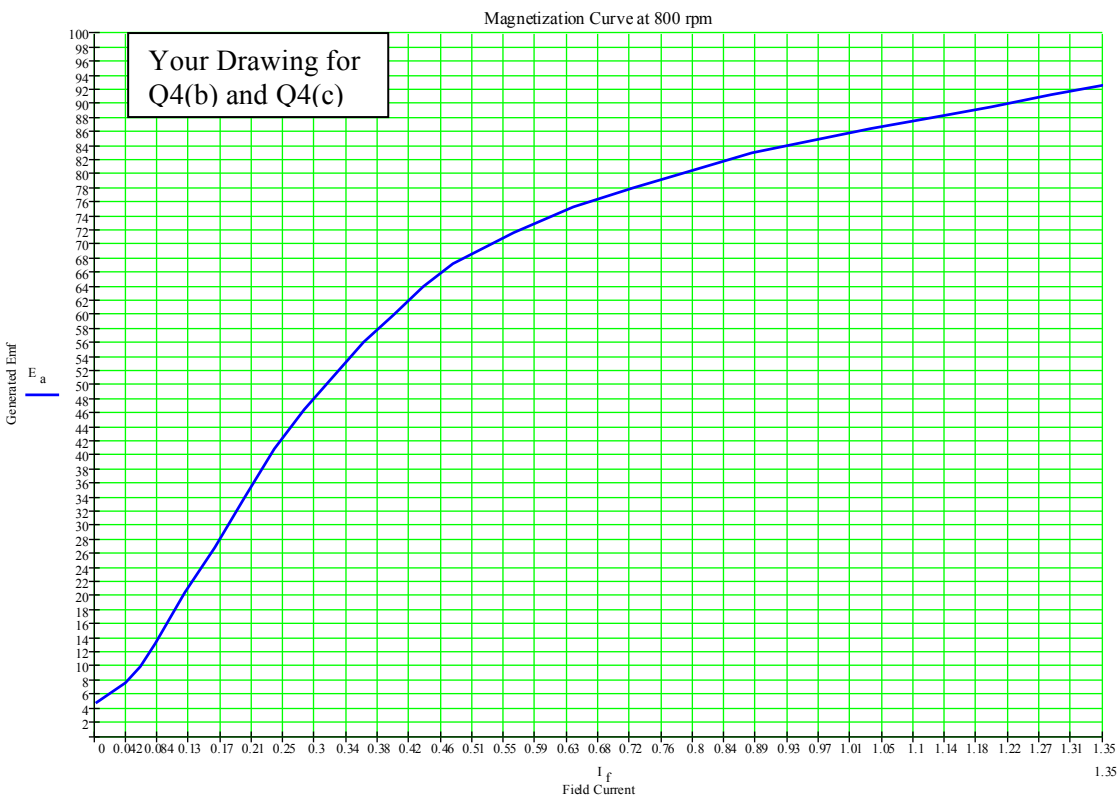
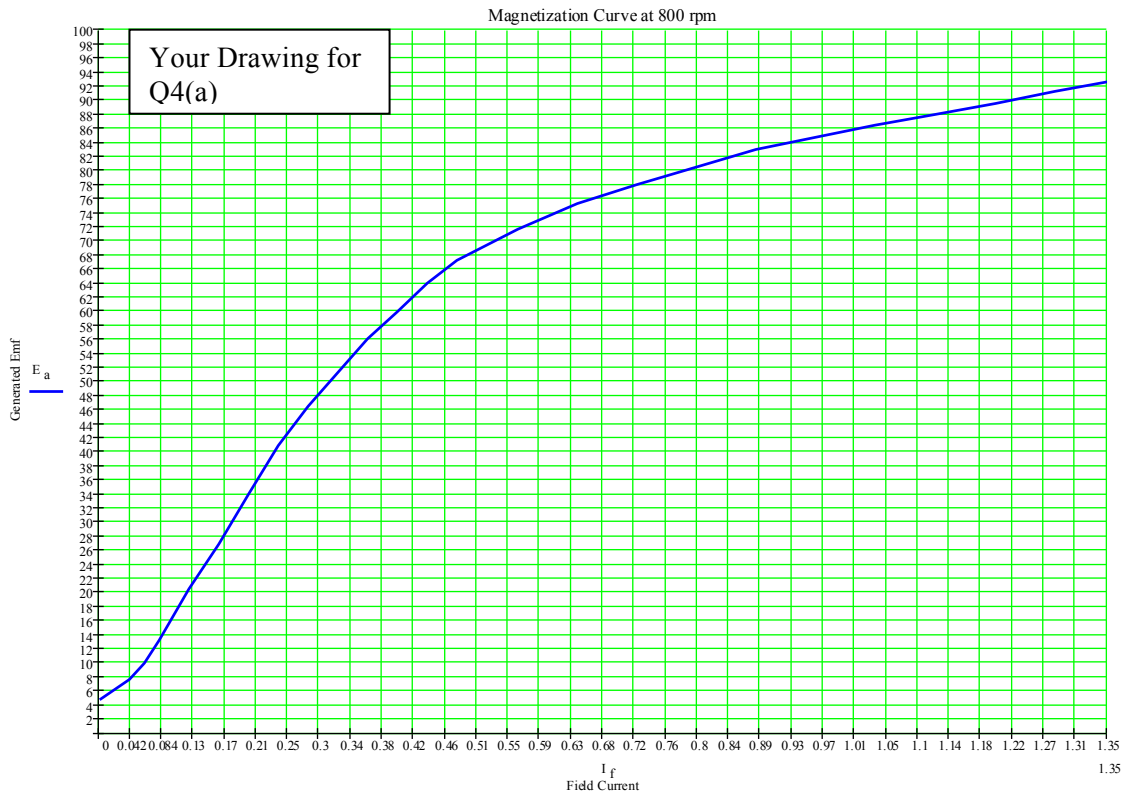
The machine is operated as a self-excited shunt dc generator at 800 rpm.

- (a) Determine the maximum and minimum values of the no-load terminal voltage, if the field control resistance,  $R_{fc}$ , whose value can be changed from 0 to 165  $\Omega$ . [2 marks]
- (b)  $R_{fc}$  is adjusted to provide a no load terminal voltage of 84 V. Determine the values of  $R_{fc}$ . [2 marks]
- (c) Determine the critical field circuit resistance. [2 marks]
- (d) The no-load terminal voltage is adjusted to 90 V. Determine the full load terminal voltage. Neglect armature reaction effects. [2 marks]
- (e) Repeat (d), assuming that the effect of armature reaction at full load is equivalent to 0.075 A field amperes, that is,  $I_{f(AR)} = 0.075$  A. [2 marks]

**Don't forget to submit Figure Q4 on page 3**

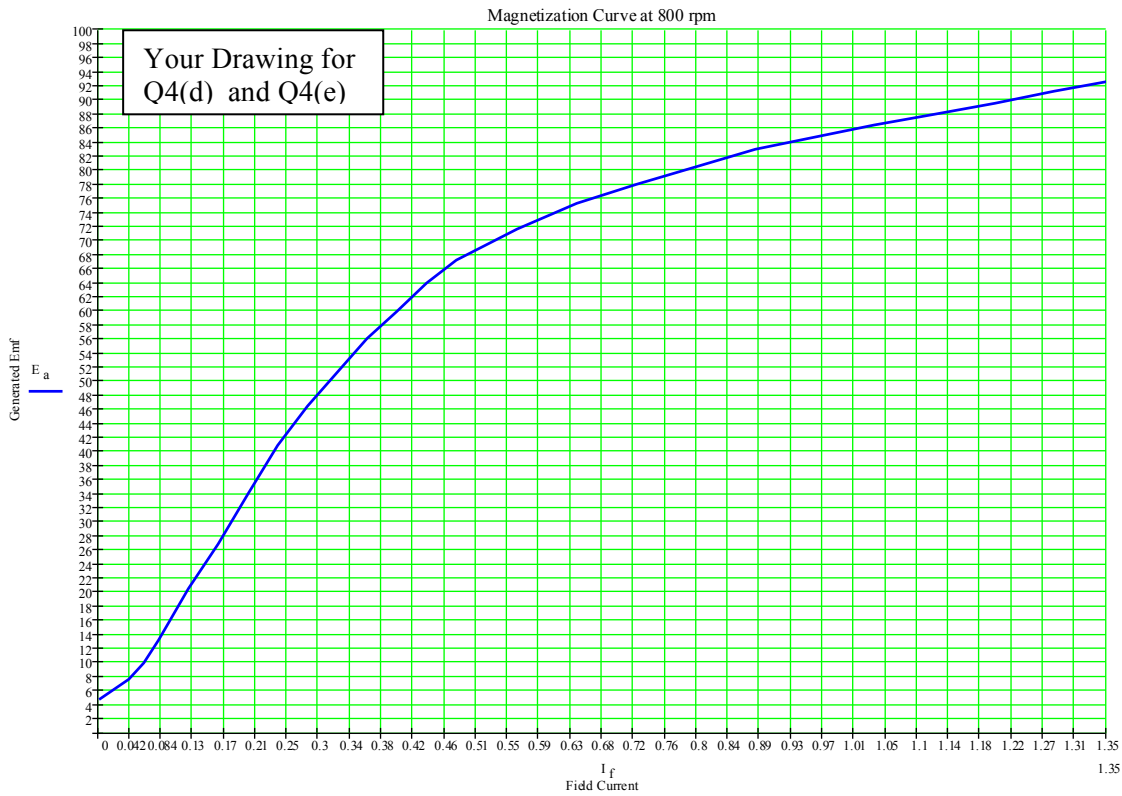
You have to submit this page!

Your name:.....



You have to submit this page!

Your name:.....



**List of Potentially useful Formula:**

$\mu_o = 4\pi \times 10^{-7}$	$W_f = \int_0^{\lambda} i d\lambda$	$f_m = - \left. \frac{\partial W_f(\lambda, x)}{\partial x} \right _{\lambda=\text{constant}}$
$B = \frac{\phi}{A} = \mu H$	$W'_f = \int_0^i \lambda di$	$f_m = \left. \frac{\partial W'_f(i, x)}{\partial x} \right _{i=\text{constant}}$
$R = \frac{l}{\mu A}$	$w_f = \int_0^B H dB$	$K_a = \frac{Np}{\pi a}$
$Hl = Ni$ $\phi R = Ni$	$w'_f = \int_0^H B dH$	$E_a = K_a \phi \omega_m$
$L \equiv \frac{\lambda}{i} = \frac{N\phi}{i} = \frac{N^2}{R}$	$W_f = \frac{1}{2} i^2 L(x)$	$T = K_a \phi I_a$
$\lambda \equiv N\phi = Li$	$f_m = \frac{i^2}{2} \frac{d}{dx} L(x)$	$V_t = R_f I_f$
$P = T\omega_m = E_a I_a$		$V_t = E_a - R_a I_a$